

CEM03 and LAQGSM03: Extension of the CEM2k+GEM2 and LAQGSM Codes to Describe Photo-Nuclear Reactions at Intermediate Energies (30 MeV to 1.5 GeV)

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The improved Cascade-Exciton Model (CEM) code CEM2k+GEM2 and the Los Alamos version of the Quark-Gluon String Model code LAQGSM are extended to describe photonuclear reactions. First, we incorporate new evaluations of elementary cross sections based on the latest experimental data into CEM2k+GEM2 and also make several improvements in the description of the de-excitation of nuclei remaining after the cascade stage of reactions induced by arbitrary projectiles. Next, for photonuclear reactions we include a normalization to evaluated experimental absorption cross sections based on the recent systematics by Kossov in CEM2k+GEM2. Then, we extend our high-energy code LAQGSM by adding the photonuclear mode which was ignored in all its previous versions, and add to it the photonuclear part from our improved CEM2k+GEM2. Presently, these codes do not include a calculation for GDR and describe properly photonuclear reactions only at intermediate energies from ~ 30 MeV to ~ 1.5 GeV. In this work we present a short description of the photonuclear mode as incorporated into our codes, show several illustrative results, and point out some unresolved problems.

1. Introduction

The 2003 version¹⁻³ of the improved⁴ Cascade-Exciton Model (CEM)⁵ as realized in the code CEM2k merged⁶⁻⁸ with the Generalized Evaporation Model code GEM2 by Furihata⁹ and of the Los Alamos version of the Quark-Gluon String Model code LAQGSM¹⁰ merged⁶⁻⁸ with GEM2 have been recently incorporated into the transport codes MARS15¹¹ and LAHET3¹² and are planned to be incorporated in the future into the transport codes MCNPX¹³ and MCNP6.¹⁴ Initially, neither CEM2k+GEM2 nor LAQGSM+GEM2 considered photonuclear reactions and were not able to describe such reactions, either as stand-alone codes or as event generators in transport codes. To address this problem, here we extend CEM03 (the 2003 version of CEM2k+GEM2) and LAQGSM03 (the 2003 version of LAQGSM+GEM2) codes to describe photonuclear reactions at intermediate energies (from ~ 30 MeV to ~ 1.5 GeV). We develop a model that is based on the Dubna IntraNuclear Cascade (INC) Photonuclear Reaction Model (PRM),¹⁵⁻¹⁷ uses experimental data now available in the literature, and a revision of recent systematics for the total photoabsorption cross sections by Kossov.¹⁸ Our photonuclear reaction model still has some problems and is under further development, but even the current version allows us to describe reasonably well intermediate energy photonuclear reactions. In the following, we present a description of our model together with several illustrative results.

2. Dubna Photonuclear Reaction Model

The Dubna intranuclear cascade photonuclear reaction model (Dubna INC) was initially developed 35 years ago by one of us (KKG) in collaboration with Iljinov and Toneev¹⁵ to describe photonuclear reactions at energies above the Giant Dipole Resonance (GDR) region. [At photon energies $T_\gamma = 10-40$ MeV, the de Broglie wavelength λ is of the order of 20-5 fm, greater than the average inter-nucleonic distance in

the nucleus; the photons interact with the nuclear dipole resonance as a whole, thus the INC is not applicable.] Below the pion production threshold, the Dubna INC considers absorption of photons on only "quasi-deuteron" pairs according to the Levinger model:¹⁹

$$\sigma_{\gamma A} = L \frac{Z(A-Z)}{A} \sigma_{\gamma d}, \quad (1)$$

where A and Z are the mass and charge numbers of the nucleus, $L \approx 10$, and $\sigma_{\gamma d}$ is the total photoabsorption cross section on deuterons as defined from experimental data.

At photon energies above the pion-production threshold, the Dubna INC considers production of one or two pions; the concrete mode of the reaction is chosen by the Monte Carlo method according to the partial cross sections (defined from available experimental data):

$$\gamma + p \rightarrow p + \pi^0, \quad (2)$$

$$\rightarrow n + \pi^+, \quad (3)$$

$$\rightarrow p + \pi^+ + \pi^-, \quad (4)$$

$$\rightarrow p + \pi^0 + \pi^0, \quad (5)$$

$$\rightarrow n + \pi^+ + \pi^0. \quad (6)$$

The cross sections of $\gamma + n$ interactions are derived from consideration of isotopic invariance, i.e. it is assumed that $\sigma(\gamma + n) = \sigma(\gamma + p)$. The Compton effect on intranuclear nucleons is neglected, as its cross section is less than $\approx 2\%$ of other reaction modes (see, e.g. Figure 6.13 in Reference 20). The Dubna INC does not consider processes involving production of three and more pions; this limits the model applicability to photon energies $T_\gamma \lesssim 1.5$ GeV [for T_γ higher than the threshold for three-pion production, the sum of the cross sections (4)–(6) is assumed to be equal to the difference between the total inelastic $\gamma + p$ cross section and the sum of the cross sections of the two-body reactions (2)–(3)].

The kinematics of two-body reactions (2)–(3) and absorption of photons by a pair of nucleons is completely defined by a given direction of emission of one of the secondary particles. Similarly to the procedure followed for $N + N$ and $\pi + N$ inter-

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actions,^{21, 22} the cosine of the angle of emission of secondary particles can be represented in the center of mass (c.m.) system as a function of a random number ξ , distributed uniformly in the interval [0,1]

$$\cos \theta = 2\xi^{1/2} \left[\sum_{n=0}^N a_n \xi^n + (1 - \sum_{n=0}^N a_n) \xi^{N+1} \right] - 1, \quad (7)$$

where $N = M = 3$,

$$a_n = \sum_{k=0}^M a_{nk} T_\gamma^k, \quad (8)$$

where the coefficients a_{nk} were fitted to describe the available experimental data and are published in Tables 1 and 2 of Reference 17 (the corresponding coefficients for $N + N$ and $\pi + N$ interactions are published in Table 3 of Reference 22 and in Table 72 of the monograph by Barashenkov and Toneev¹⁶). The distribution of the secondary particles over the azimuthal angle φ is assumed to be isotropic. After simulating the angle Θ_1 , using eqs 7 and 8, and φ_1 isotropically for the first particle of any reaction with two particles in the final state, the angles Θ_2 and φ_2 of the second particle, as well as the energies of both particles T_1 and T_2 are uniquely determined from four-momentum conservation.

The analysis of experimental data has shown that the channel (4) of two-pion photoproduction proceeds mainly through the decay of the Δ^{++} isobar listed in the last Review of Particle Physics by the Particle Data Group²³ as having the mass $M = 1232$ MeV



whereas the production cross section of other isobar components ($\frac{3}{2}, \frac{3}{2}$) are small and can be neglected. The Dubna INC uses the Lindenbaum-Sternheimer resonance model²⁴ to simulate the reaction (9). In accordance with this model, the mass of the isobar M is determined from the distribution

$$\frac{dW}{dM} \sim F(E, M) \sigma(M), \quad (10)$$

where E is the total energy of the system, F is the two-body phase space of the isobar and π^- meson, and σ is the isobar production cross section which is assumed to be equal to the cross section for elastic π^+p scattering.

The c.m. emission angle of the isobar is approximated using eqs 7 and 8 with the coefficients a_{nk} listed in Table 3 of Reference 17; isotropy of the decay of the isobar in its c.m. system is assumed.

In order to calculate the kinematics of the non-resonant part of the reaction (4) and two remaining three-body channels (5) and (6), the Dubna INC uses the statistical model. The total energies of the two particles (pions) in the c.m. system are determined from the distribution

$$\frac{dW}{dE_{\pi_1} dE_{\pi_2}} \sim (E - E_{\pi_1} - E_{\pi_2}) E_{\pi_1} E_{\pi_2} / E, \quad (11)$$

and that of the third particle (nucleon, N) from conservation of energy. The actual simulation of such reactions is done as follows: Using a random number ξ , we simulate in the beginning the energy of the first pion using

$$E_{\pi_1} = m_{\pi_1} + \xi(E_{\pi_1}^{\max} - m_{\pi_1}),$$

where

$$E_{\pi_1}^{\max} = [E^2 + m_{\pi_1}^2 - (m_{\pi_2} + m_N)^2] / 2E.$$

Then, we simulate the energy of the second pion E_{π_2} according to eq 11 using the Monte Carlo rejection method. The energy of the nucleon is then calculated as $E_N = E - E_{\pi_1} - E_{\pi_2}$, checking

that the ‘‘triangle law’’ for momenta

$$|p_{\pi_1} - p_{\pi_2}| \leq p_N \leq |p_{\pi_1} + p_{\pi_2}|$$

is fulfilled, otherwise this sampling is rejected and the procedure is repeated. The angles Θ and φ of the pions are sampled assuming an isotropic distribution of particles in the c.m. system,

$$\begin{aligned} \cos \Theta_{\pi_1} &= 2\xi_1 - 1, & \cos \Theta_{\pi_2} &= 2\xi_2 - 1, \\ \varphi_{\pi_1} &= 2\pi \xi_3, & \varphi_{\pi_2} &= 2\pi \xi_4, \end{aligned}$$

and the angles of the nucleon are defined from momentum conservation, $\vec{p}_N = -(\vec{p}_{\pi_1} + \vec{p}_{\pi_2})$.

So an interaction of a photon with a nucleon inside a nucleus leads to two or three fast cascade particles. Depending on their momenta and coordinates, these particles can leave the nucleus, be absorbed, or initiate a further intranuclear cascade. All the remaining details of the Dubna INC (followed by the evaporation/fission of excited nuclei produced after the cascade stage of reactions) calculation are the same as for $N+A$ and $\pi+A$ reactions and are described in detail in the monograph.¹⁶

The Dubna INC PRM was used successfully for many years as a stand-alone model to study different aspects of photonuclear reactions and was also incorporated without modifications into the transport codes CASCADE²⁵ and GEANT4,²⁶ and with some improvements, via CEM95,²⁷ CEM97,²⁸ and CEM2k,⁴ into the transport codes MARS14²⁹ and MCNPX,^{13, 30, 31} respectively. In the middle of the 1970s, one of the authors of the initial version of the Dubna INC PRM, Iljinov, moved from JINR, Dubna to INR, Moscow and continued to develop further the Dubna INC with his Moscow Group, which evolved into what is now known in the literature as the Moscow INC model (see, e.g. Reference 32 and references therein). The Moscow INC model was recently extended to describe photonuclear reactions at energies up to 10 GeV.³³

3. From CEM95 to CEM03

Photonuclear reactions were not considered in the initial version of the CEM.⁵ The Dubna PRM was incorporated³⁴ first into the CEM95²⁷ version of the CEM and used thereafter to analyze a large number of photonuclear reactions.³⁵ Later on, CEM95 was incorporated as an event generator into the MARS14²⁹ transport code and used in some applications.

By early 1997, one of the authors of the CEM (SGM) moved from JINR, Dubna to LANL, Los Alamos, and continued to develop further with his collaborators the cascade-exciton model for LANL needs, e.g. as an event generator for the Los Alamos transport code MCNPX¹³ and for other applications.

3.1. New Approximations for γp Cross Sections. The first improvements in the CEM of the photonuclear mode of the Dubna INC was done in the CEM97 version²⁸ of the CEM. The improved cascade-exciton model in the code CEM97 differs from the older CEM95 version by incorporating new approximations for the elementary NN , πN , and γp cross sections used in the cascade, using more precise values for nuclear masses and pairing energies, employing a corrected systematics for the level-density parameters, adjusting the cross sections for pion absorption on quasi-deuteron pairs inside a nucleus, including the Pauli principle in the preequilibrium calculation, and improving the calculation of fission widths. Implementation of significant refinements and improvements in the algorithms of many subroutines led to a decrease of the computing time by up to a factor of 6 for heavy nuclei, which is very important when performing simulations with transport codes.

Concerning specifically the photonuclear reactions, in CEM97 we developed improved approximations for the elementary γp cross sections compared with the Dubna INC PRM.¹⁵

In the Dubna INC PRM¹⁵ used in CEM95, the cross sections for the free γp (and for NN and πN) interactions are approximated using a special algorithm of interpolation/extrapolation through a number of picked points, mapping the experimental data as possible. This was done very accurately by the authors of the Dubna INC PRM¹⁵ using all experimental data available at that time, about 35 years ago. Currently there are many more experimental data on cross section; therefore we revised the approximations of all elementary cross sections used in CEM97.²⁸ We collected all published experimental data from available sources, then developed an improved algorithm for approximating cross sections and developed simple and fast approximations for elementary cross sections which fit very well presently available experimental data not only up to ~ 1.5 GeV, where the Dubna INC PRM is assumed to be used, or up to about 5 GeV, the upper recommended energy for the present version of the CEM for nucleon- and pion-induced reactions, but up to 50–100 GeV and higher, depending on availability of data. So far we have such approximations for 8 different

types of $\gamma + p$ elementary cross sections and for 24 types of reactions induced by nucleons and pions. Cross sections for other types of interactions taken into account by CEM are calculated from isospin considerations using the former as the input. These cross sections are used in CEM97,²⁸ CEM2k,⁴ and CEM03,¹ and were incorporated recently into the latest version of our LAQGSM¹⁰ code, LAQGSM03.^{1,2}

We consider this part of the CEM improvement as an independently useful development, as our approximations are reliable, fast, and easy to incorporate into any transport, INC, BUU, or Glauber-type model codes. For example, our new approximations recently have been successfully incorporated by Mokhov into the MARS14²⁹ and MARS15¹¹ versions of the MARS code system at Fermilab.

An example of 8 compiled $\gamma + p$ experimental cross sections together with our new CEM03 approximations and the old approximations from the Dubna INC PRM used in CEM95 is shown in Figure 1. We see that these approximations describe all data very well. Although presently we have much more

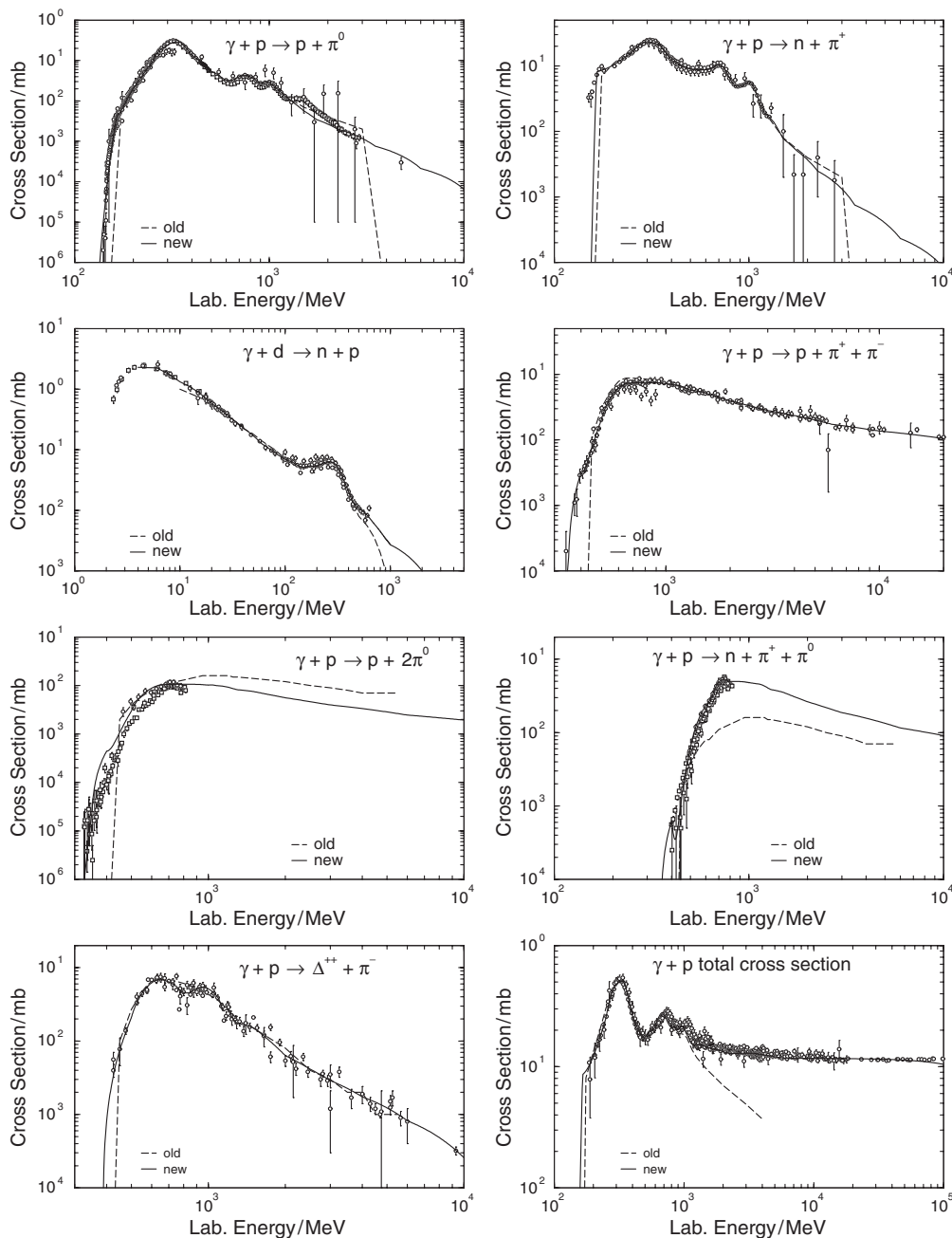


Figure 1. Comparison of eight experimental total $\gamma + p(d)$ cross sections with the old approximations from the Dubna INC PRM and with our new approximations incorporated into the CEM03 and LAQGSM03 codes. Experimental data (circles and squares) are compiled from: $\gamma + p \rightarrow p + \pi^0$: Refs. 36–45; $\gamma + p \rightarrow n + \pi^+$: Refs. 36–39 and 46–51; $\gamma + d \rightarrow n + p$: Refs. 23, 37, and 52–72; $\gamma + p \rightarrow p + \pi^+ + \pi^-$: Refs. 37, 42, and 73–76; $\gamma + p \rightarrow p + 2\pi^0$: Refs. 73 and 77–79; $\gamma + p \rightarrow n + \pi^+ + \pi^0$: Refs. 73, 80, and 81; $\gamma + p \rightarrow \Delta^{++} + \pi^-$: Ref. 37; $\gamma + p$ total cross sections: Refs. 23, 37, 51, and 52, respectively. The squares show recent experimental data that became available to us after we completed our fit; although these recent data agree reasonably well with our approximations, a re-fitting would slightly improve the agreement.

data than 35 years ago when the Dubna group produced their approximations used in the Dubna INC PRM,¹⁵ for a number of interaction modes like the total γp cross sections at energies below 1.2 GeV (where the initial Dubna INC PRM was assumed to be used), and for such modes as $\gamma + p \rightarrow p + \pi^0$, $\gamma + p \rightarrow n + \pi^+$, $\gamma + p \rightarrow p + \pi^+ + \pi^-$, and $\gamma + d \rightarrow n + p$, at energies not too close to their thresholds, the original approximations also agree very well with presently available data, in the energy region where the Dubna INC PRM was developed to work. This is a partial explanation of why the old Dubna INC¹⁶ and the younger CEM95²⁷ describe so well many characteristics of different nuclear reactions. On the other hand, for some elementary cross sections like $\gamma + p \rightarrow p + 2\pi^0$ and $\gamma + p \rightarrow n + \pi^+ + \pi^0$, the old approximations differ significantly from the present data, demonstrating the need for a better description of all modes of photonuclear reactions. (Similar results were obtained in CEM97²⁸ for hadron-hadron cross section approximations.)

The CEM97 code with these cross sections and the other mentioned improvements was incorporated by Gallmeier³⁰ into the MCNPX transport code,¹³ allowing MCNPX to consider for the first time interaction of intermediate-energy photons with thick targets of practically arbitrary geometry.

3.2. New Approximations for Differential $\gamma + p$ Cross Sections. The CEM2k⁴ version of CEM is a “new generation” of the CEM following CEM97.²⁸ Its development was partially

motivated by the availability of some new, very precise and useful experimental data obtained recently at GSI in Darmstadt, Germany, where a large number of measurements have been performed using inverse kinematics for interactions of ^{56}Fe , ^{197}Au , ^{208}Pb , and ^{238}U at 1500, 1000, 800, 750, 500, and 300 MeV/nucleon with liquid ^1H . These measurements provide a large set of cross sections for production of practically all possible isotopes from such reactions in a “pure” form, i.e. individual cross sections from a specific given bombarding isotope (or target isotope, when considering reactions in the usual kinematics, $p + A$). Such cross sections are much easier to compare to models than the “camouflaged” data from γ -spectrometry measurements. In addition, many reactions where a beam of light, medium, or heavy ions with energy near to or below 1 GeV/nucleon interact with different nuclei, from the lightest, d, to the heaviest, ^{208}Pb , were measured recently at GSI. References on these measurements and many tabulated experimental cross sections may be found on the Web page of Schmidt.⁸²

(We have analyzed with CEM2k and LAQGSM all measurements done at GSI of which we are aware, both for proton-nucleus and nucleus-nucleus interactions; some examples of our results compared with the GSI data and calculations by other available models may be found in Reference 3 and references therein.)

During the development of the CEM2k version of CEM and

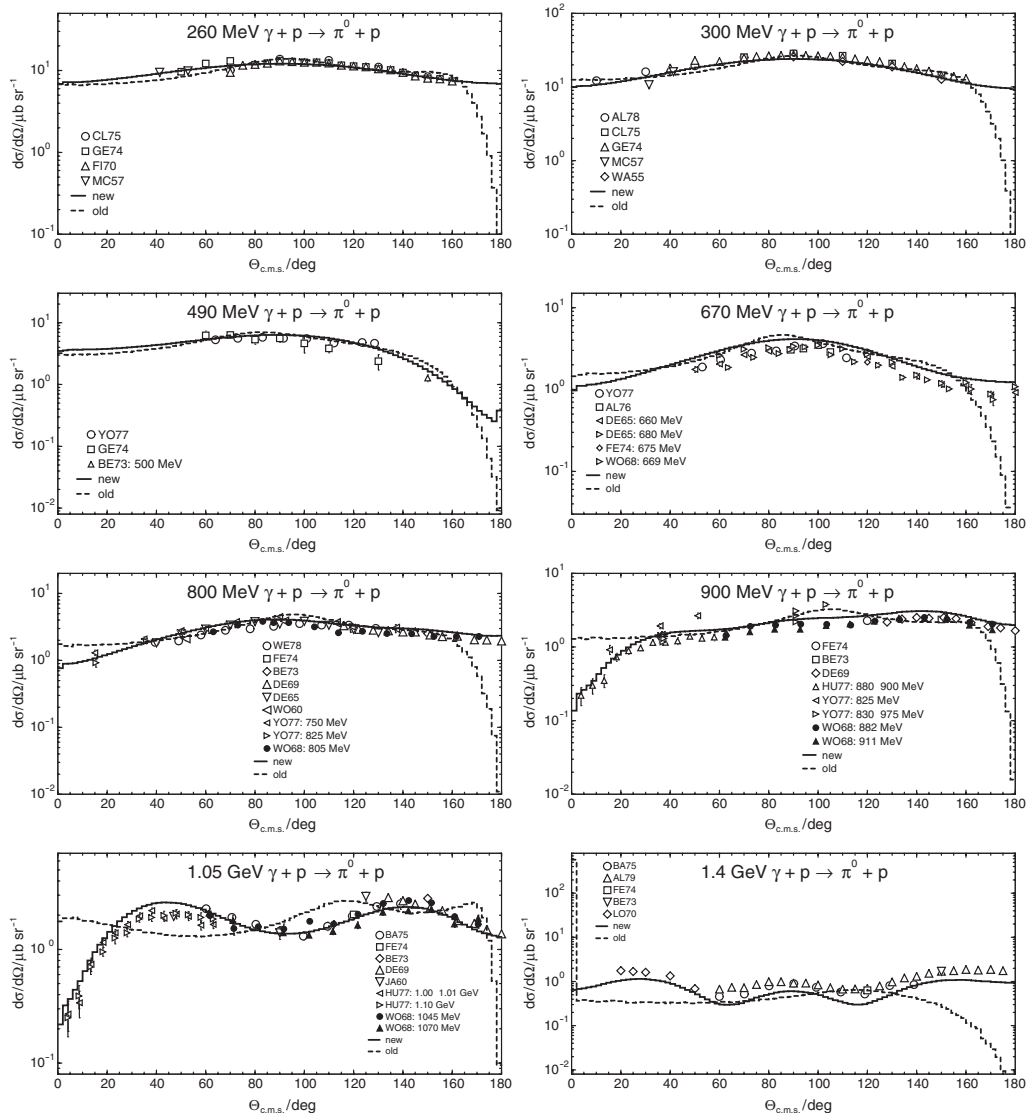


Figure 2. Example of eight angular distributions of π^0 from $\gamma p \rightarrow \pi^0 p$ as functions of $\Theta_{c.m.s.}^{\pi}$ at photon energies from 260 MeV to 1.4 GeV. The dashed lines show the old approximations of the Dubna INC PRM while the solid lines are our new approximations incorporated into the CEM03 and LAQGSM03 codes. Experimental data are shown by symbols and are from: CL75,⁸³ GE74,⁸⁴ FI70,⁸⁵ MC57,⁸⁶ AL78,⁸⁷ WA55,⁸⁸ YO77,⁸⁹ BE73,⁹⁰ AL76,⁹¹ DE65,⁹² FE74,⁹³ WO68,⁹⁴ WE78,⁹⁵ DE69,⁹⁶ WO60,⁹⁷ HU77,⁹⁸ BA75,⁹⁹ JA60,¹⁰⁰ AL79,¹⁰¹ and LO70;¹⁰² tabulated values are available at: <http://www.spires.dur.ac.uk/hepdata/react2.html>.

of LAQGSM, we concentrated mainly on proton-nucleus and nucleus-nucleus reactions and tried to improve the general description of different types of nuclear reactions by our models, without focusing specifically on photonuclear reactions. The main difference of CEM2k from its precursor CEM97 is in the criterion for when to move from the intranuclear-cascade stage of a reaction to its preequilibrium stage, and when to move from the latter to the evaporation/fission slow stage of the reaction. In short, CEM2k has a longer cascade stage, less preequilibrium emission, and a longer evaporation stage with a higher excitation energy, as compared to CEM97 and CEM95. Besides these changes to CEM97, we also made in CEM2k a number of other improvements and refinements, such as imposing momentum-energy conservation for each simulated event (the Monte Carlo algorithm previously used in CEM provides momentum-energy conservation only statistically, on the average, but not exactly for each simulated event); using real binding energies for nucleons at the cascade stage of a reaction instead of the approximation of a constant separation energy of 7 MeV used in the previous versions of the CEM; using reduced masses of particles in the calculation of their emission widths instead of using the approximation of no recoil used in the previous versions; and coalescence of complex particles from fast cascade nucleons already outside the nucleus. On the whole, CEM2k describes many nuclear reactions, including the ones induced by photons better than CEM97 and CEM95 do. CEM2k was incorporated

by Gallmeier into MCNPX to replace CEM97, and this version of MCNPX was extended by him to describe photonuclear reactions also in the GDR region³¹ (as a stand-alone code, CEM2k was developed to describe photonuclear reactions only at energies above the GDR region).

We have focused on the improved description of specifically the photonuclear reactions when developing our latest version of CEM, CEM03.¹ Although CEM97 contained new approximations and algorithms to better describe the integrated elementary NN , πN , and γN cross sections as mentioned above, the double differential distributions of secondary particles from such interactions were simulated by CEM2k and all its precursors using the old Dubna INC approximations (7)–(11) for γp reactions (and similar relations, for NN and πN collisions). These were obtained by Gudima et al.^{15, 21, 22} 36 years ago, using the measurements available at that time. In CEM03, for NN and πN collisions, we addressed this problem by developing new approximations similar to (7)–(11) and by using recent systematics by other authors, based on the experimental data available today (see details on NN and πN reactions in Reference 1). In the case of γp reactions (2) and (3), we chose another way: Instead of fitting the parameters a_n from eq 7 at different E_γ we found data (see, e.g. Figures 2 and 3) and finding the energy dependence of parameters a_{nk} in eq 8 using the values obtained for a_n as was done in the old Dubna INC, we took advantage of the event generator for γp and γn reactions from the Moscow

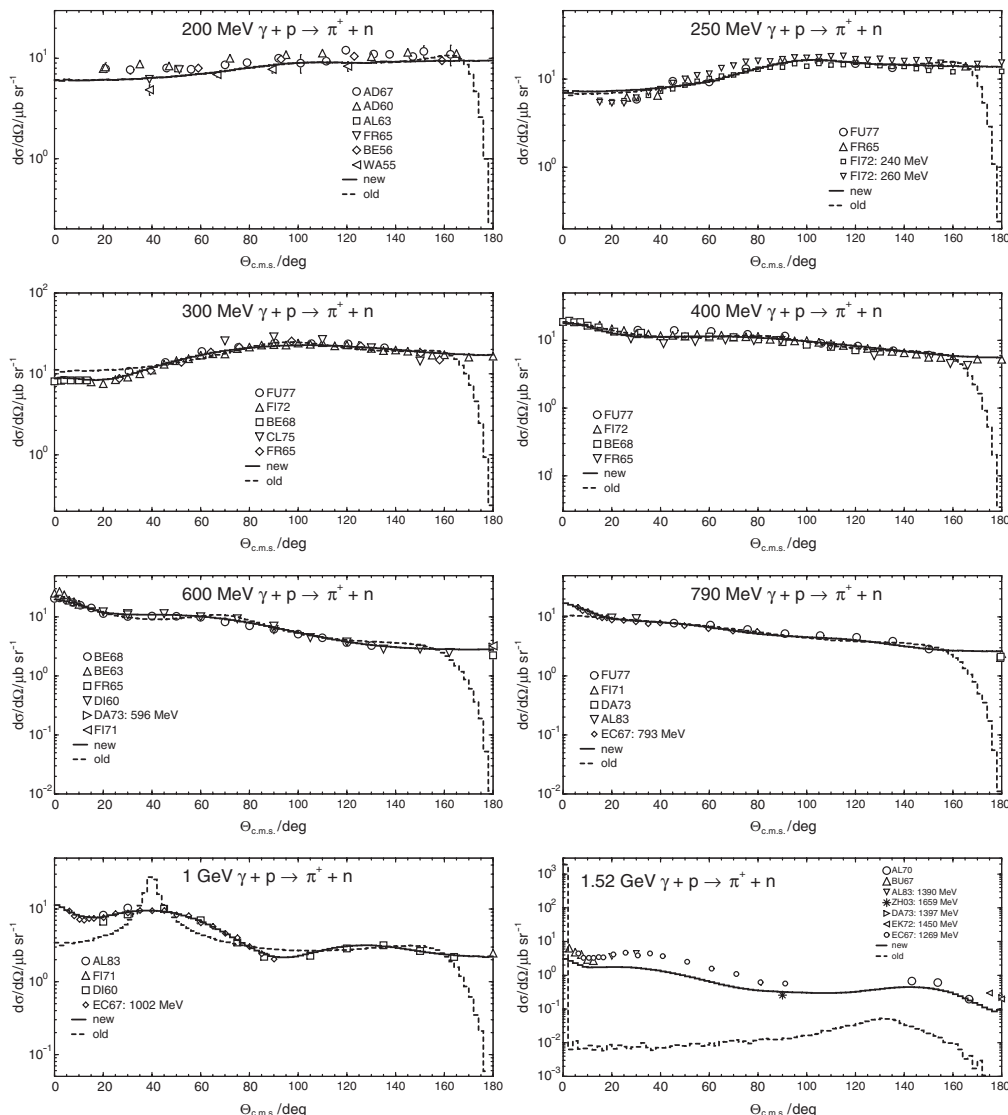


Figure 3. Example of eight angular distributions of π^+ from $\gamma p \rightarrow \pi^+ n$ as functions of $\Theta_{c.m.s.}^\pi$ at photon energies from 200 MeV to 1.52 GeV. The dashed lines show the old approximations of the Dubna INC PRM while the solid lines are our new approximations incorporated into the CEM03 and LAQGSM03 codes. Experimental data are shown by symbols and are from: AD67,¹⁰³ AD60,¹⁰⁴ AL63,¹⁰⁵ FR65,¹⁰⁶ BE56,¹⁰⁷ WA55,¹⁰⁸ FU77,¹⁰⁹ FI72,¹¹⁰ BE68,¹¹¹ CL75,⁸³ BE63,¹¹² DI60,¹¹³ DA73,¹¹⁴ FI71,¹¹⁵ AL83,¹¹⁶ EC67,¹¹⁷ AL70,¹¹⁸ BU67,¹¹⁹ ZH03,¹²⁰ and EK72;¹²¹ tabulated values are available at: <http://wwwSPIRES.dur.ac.uk/hepdata/reac2.html>.

INC³³ kindly sent us by Pshenichnov. That event generator includes a data file with smooth approximations through presently available experimental data at 50 different gamma energies from 117.65 to 6054 MeV (in the system where the p or n interacting with γ is at rest) for the c.m. angular distributions $d\sigma/d\Omega$ of secondary particles as functions of Θ tabulated for values of Θ from 0 to 180° with the step $\Delta\Theta = 10^\circ$ for 60 different channels of γp and γn reactions considered by the Moscow INC (see details in Reference 33). We use part of that data file with data for reactions (2) and (3), and have written an algorithm to simulate unambiguously $d\sigma/d\Omega$ and to choose the corresponding value of Θ for any E_γ , using a single random number ξ uniformly distributed in the interval [0,1]. This is straightforward due to the fact that the function $\xi(\cos \Theta)$

$$\xi(\cos \Theta) = \int_{-1}^{\cos \Theta} d\sigma/d\Omega d\cos \Theta \Big/ \int_{-1}^1 d\sigma/d\Omega d\cos \Theta$$

is a smooth monotonic function increasing from 0 to 1 as $\cos \Theta$ varies from -1 to 1 . Naturally, when E_γ differs from the values tabulated in the data file, we perform first the needed interpolation in energy. We use this procedure to describe angular distributions of secondary particles from reactions (2) and (3), as well as for isotopically symmetric reactions $\gamma + n \rightarrow n + \pi^0$ and $\gamma + n \rightarrow p + \pi^-$ in CEM03.

Examples of eight angular distributions of π^0 from $\gamma p \rightarrow \pi^0 p$ and of π^+ from $\gamma p \rightarrow \pi^+ n$ as functions of $\Theta_{c.m.s}^\pi$ are presented in Figures 2 and 3. We see that the approximations developed in CEM03 (solid histograms) agree much better with the available experimental data than the old Dubna INC approximations (7)–(8) used in all precursors of CEM03 (dashed histograms).

4. New Approximations for $\gamma + A$ Absorption Cross Sections

CEM03 (and its predecessors) does not consider absorption of low energy photons in the GDR region and takes into account photoproduction on free nucleons of only two pions. This restricts its applicability to the range $30 \text{ MeV} \lesssim E_\gamma \lesssim 1.5 \text{ GeV}$, which is not convenient when it is used as an event generator in a transport code.

To extend the applicability of CEM03 (and LAQGSM03) into the GDR region, it is necessary to omit the intranuclear cascade (INC) and to consider such reactions as starting with the preequilibrium model. The INC used by CEM03 as the first stage of arbitrary reactions is a semiclassical model that does not consider any collective degrees of freedom of a nucleus, including the GDR; in addition, the photon-energy in the GDR region is too low to justify the use of any INC. In our approach, it is possible to deal with this limitation as was done 30 years ago,¹²² using the Modified Exciton Model (MEM)^{123, 124} used in the initial version of CEM⁵ and 25 years later,¹²⁵ using an improved version of the MEM contained in the CEM95²⁷ code. We plan to extend CEM03 to describe photonuclear reactions in the GDR region in the near future, but this requires a large amount of tedious work: 1) to make sure that we use the most reliable parameters of the GDR for all nuclei, 2) to define an optimal transition from the current three-stage (INC, preequilibrium, and evaporation/fission) description of reactions to a two-stage approach needed in the GDR region, and 3) to test the extended model against the available experimental data.

To describe properly with CEM03 and LAQGSM03 photonuclear reactions above $E_\gamma \sim 1.5 \text{ GeV}$, it is necessary to take into account production of more than two pions in γN collisions, as well as to consider production of resonances heavier than $\Delta(1232)$, as has been done, i.e. in the Moscow INC.³³ We plan to extend CEM03 and LAQGSM03 to higher E_γ in subsequent versions.

In the meantime, it is possible to get quite reasonable results for spectra of emitted nucleons and complex particles and for

the nuclide production cross sections with our present CEM03 model for photonuclear reactions both in the GDR region and at $E_\gamma \gtrsim 1.5 \text{ GeV}$, by employing a correct total photoabsorption cross section. Indeed, CEM03 starts a reaction in the GDR region with a cascade and since the γ energy is below the pion-production threshold, the only available reaction channel is to absorb such photons on a quasi-deuteron pair of nucleons, generating two “cascade” nucleons inside the nucleus. As the energy of these nucleons is low, $\sim 10 \text{ MeV}$, these nucleons are “absorbed” by the nucleus generating two excited nucleons (excitons) and two holes, then CEM03 would proceed with this process as a preequilibrium reaction followed by evaporation/fission. All the real calculation of such reactions would be done with only the preequilibrium and evaporation models and the INC would serve only to provide the number of excitons, as an input to the MEM. At the end of the calculation, the total photoabsorption (reaction) cross section is needed to normalize the results. CEM03 (and most other INC models) calculates the total reaction cross section, σ_{in} , by the Monte Carlo method using the geometrical cross section, σ_{geom} , and the number of inelastic, N_{in} , and elastic, N_{el} , simulated events, namely: $\sigma_{in} = \sigma_{geom} N_{in} / (N_{in} + N_{el})$. This approach provides a good agreement with available data for reactions induced by nucleons, pions, and photons at incident energies above about 100 MeV, but is not reliable at energies below 100 MeV (see, e.g. Figures 3 and 4 and Reference 7).

To address this problem for photonuclear reactions, we have written a FORTRAN routine called GABS.FOR based on the recent approximation by Kossov,¹⁸ that provides reliable photoabsorption cross sections on arbitrary targets at all energies from the hadron production threshold to about 40 TeV. We have added GABS.FOR to CEM03 to normalize our photonuclear results to this systematics rather than to σ_{in} calculated by the Monte Carlo method, as we have done previously. (As a rule, we use LAQGSM03 only at energies above several GeV, where CEM03 becomes already not reliable; at such high energies, LAQGSM03 describes quite well σ_{in} and does not require renormalization of its results to any systematics; therefore we do not incorporate GABS.FOR into LAQGSM03.)

The Kossov approximation¹⁸ of the energy dependence of photonuclear cross sections is subdivided into three main regions: the GDR region, the nucleon resonance region, and the high-energy region. Its functional form is also subdivided into three groups depending on the mass number of the target: the $\sigma_{\gamma p}$ cross section, the cross section for γd reactions, and the $\sigma_{\gamma A}$ cross section for $A > 2$.

We note that eq 41 in Reference 18 was misprinted in the original publication by Kossov, where a “+” sign occurs instead of a “–” sign. The misprinted formula does not reproduce the cross sections presented in Reference 18, whereas the corrected version does.

Figures 4 and 5 show examples of twelve photoabsorption cross sections on several light, medium, and heavy nuclei. In these figures, we compare predictions of the Kossov systematics as implemented in the routine GABS.FOR with available experimental data and with the Los Alamos National Laboratory (LANL), Korean Atomic Energy Institute (KAERI), and the Institute of Physics and Power Engineering (IPPE), Obninsk, Russia and the Center for Photonuclear Experimental Data [Centr Dannykh Fotoyasdernykh Eksprimentov (CDFE), in Russian], Moscow, Russia, Modified (MOD) Library of Photonuclear Data [Biblioteka Fotoyadernykh Dannykh (BOFOD), in Russian], BOFOD(MOD), evaluations from the IAEA Photonuclear Data Library,¹²⁶ as well as with calculations by two older versions of CEM, namely, the CEM95 photonuclear code version³⁴ and CEM2k as modified by Gallmeier³¹ for MCNPX.

The Kossov systematics describe well the experimental photoabsorption cross sections and agree with the LANL,

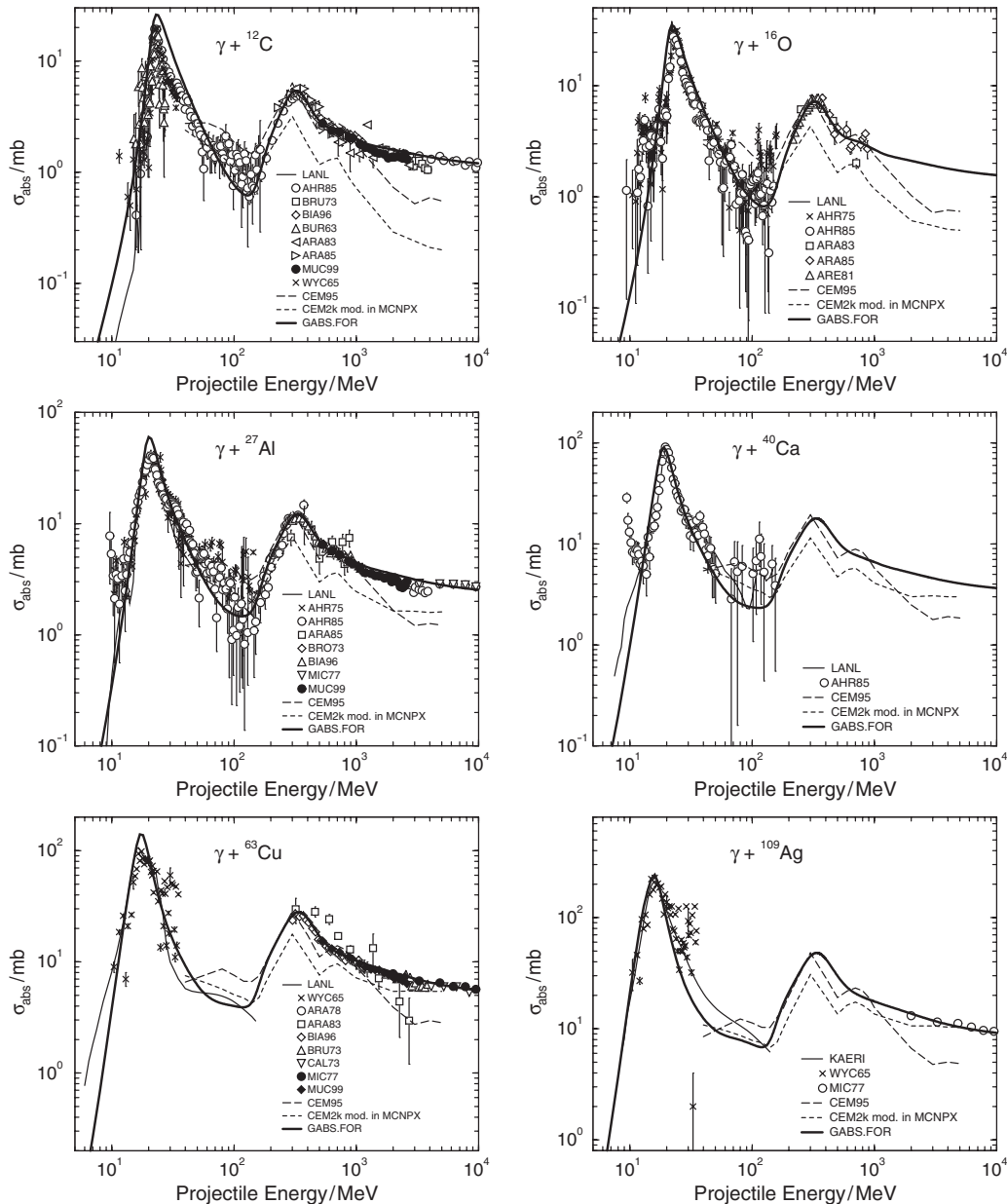


Figure 4. Examples of total photoabsorption cross sections for ^{12}C , ^{16}O , ^{27}Al , ^{40}Ca , ^{63}Cu , and ^{109}Ag as functions of photon energy. The thick solid lines marked as “GABS.FOR” are from our subroutine written to reproduce Kossov’s¹⁸ systematics, as described in the text. The thin solid line marked as “LANL” (or “KAERI”, for ^{109}Ag) show the evaluations by LANL (or KAERI, for ^{109}Ag) from the IAEA Photonuclear Data Library.¹²⁶ Results from the photonuclear version of CEM95³⁴ and from CEM2k as modified for MCNPX by Gallmeier³¹ are shown by the long-dashed and dashed lines, respectively. Experimental data (symbols) are from: AHR85,¹²⁷ BRU73,¹²⁸ BIA96,¹²⁹ BUR63,¹³⁰ ARA83,¹³¹ ARA85,¹³² MUC99,¹³³ WYC65,¹³⁴ AHR75,¹³⁵ ARE81,¹³⁶ MIC77,¹³⁷ ARA78,¹³⁸ and CAL73.¹³⁹

KAERI, and the BOFOD evaluations, especially for heavy targets. For ^{12}C , ^{27}Al , and ^{63}Cu (and several other nuclei we tested but did not include in Figures 4 and 5) the agreement in the GDR region is not so good. This is because we use here the “global” approximation given by the Kossov systematics to calculate the photoabsorption cross section in the GDR region for all nuclei. It is known from the literature that the GDR of light nuclei differ significantly from the ones of heavy nuclei, and should be addressed carefully for each light nucleus separately. In fact, Kossov¹⁸ had fitted the parameters of the light nuclei separately and his results shown in Figures 2 to 7 of Reference 18 for the light nuclei agree better with the data than the “global” systematics shown here does. Unfortunately, Kossov did not publish the parameterization of the GDR he found for every light nucleus in Reference 18 (some details of this are listed in the recent *GEANT4 Physics Reference Manual*¹⁵⁶ and in Reference 157, but only for some light nuclei, and those details differ from what is published in Reference 18). To fill this gap, we hope to determine ourselves a parameterization of the GDR photoabsorption on light nuclei using all available

experimental data.

5. Illustrative Results

In this Section, we present several illustrative results from CEM03 and LAQGSM03 extended to describe photonuclear reactions. Let us start with photofission cross sections. We have compiled from the literature all reliable experimental data on photofission cross sections that we could identify and have analyzed them with both CEM03 and LAQGSM03. Figure 6 shows a comparison of such data for ^{197}Au , ^{208}Pb , ^{209}Bi , ^{232}Th , ^{233}U , ^{235}U , ^{238}U , and ^{237}Np with the results of CEM03, as well as to several earlier versions, namely, the photonuclear versions of CEM95,³⁴ CEM98,¹⁵⁸ CEM2k+GEM2,⁸ and by the modified version of CEM2k incorporated into MCNPX by Gallmeier.³¹ The CEM03 results agree well with the experimental fission cross sections, and better than the results of the earlier models. The Kossov approximation for the total photoabsorption cross sections in CEM03 (and CEM2k+GEM2) allows us to describe the fission cross section, not only for photon energies from ~ 30

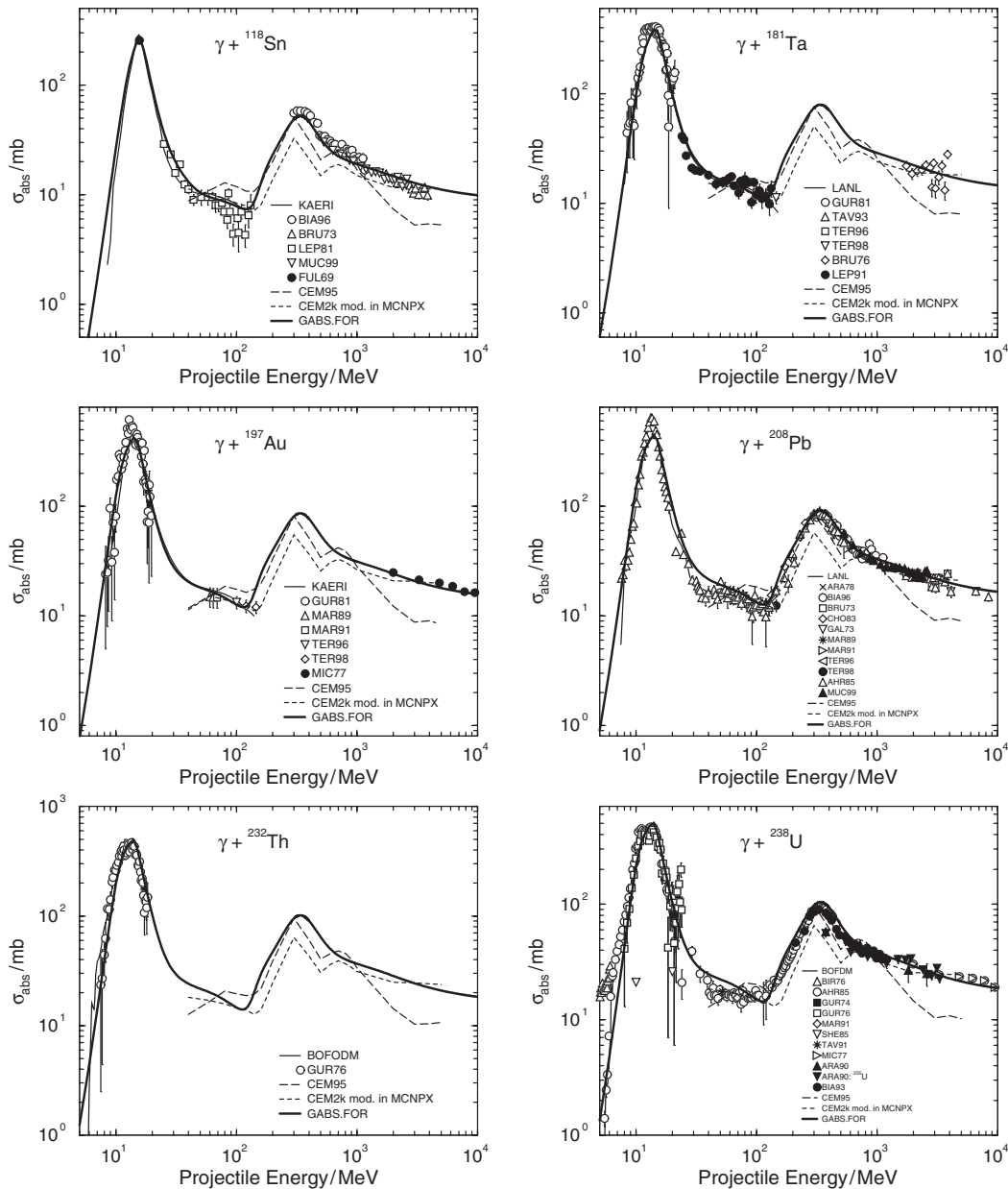


Figure 5. Examples of total photoabsorption cross sections for ^{118}Sn , ^{181}Ta , ^{197}Au , ^{208}Pb , ^{232}Th , and ^{238}U as functions of photon energy. The thick solid lines marked as “GABS.FOR” are results by our subroutine written to reproduce Kossov’s¹⁸ systematics, as described in the text. The thin solid line marked as “LANL”, “KAERI”, or “BOFODM” show the evaluations by LANL, KAERI, or by a collaboration between IPPE/Obninsk and CDFE/Moscow (the BOFOD(MOD) Library) from the IAEA Photonuclear Data Library.¹²⁶ Results from the photonuclear version of CEM95³⁴ and from CEM2k as modified for MCNPX by Gallmeier³¹ are shown by the long-dashed and dashed lines, respectively. Experimental data (symbols) are from: BIA96,¹²⁹ BRU73,¹²⁸ LEP81,¹⁴⁰ MUC99,¹³³ FUL69,¹⁴¹ GUR81,¹⁴² TAV93,¹⁴³ TER96,¹⁴⁴ TER98,¹⁴⁵ MAR91,¹⁴⁶ MAR91,¹⁴⁷ MIC77,¹³⁷ ARA78,¹³⁸ CHO83,¹⁴⁸ CAL73,¹³⁹ AHR85,¹²⁷ GUR76,¹⁴⁹ BIR76,¹⁵⁰ GUR74,¹⁵¹ SHE85,¹⁵² TAV91,¹⁵³ ARA90,¹⁵⁴ and BIA93.¹⁵⁵

MeV to ~ 1.5 GeV, where the model is expected to be reliable, but also outside this region, i.e. in the whole range from 10 MeV to 5 GeV.

This is an example of getting reasonably good results outside the region where the model is justified, as discussed in the previous section. Results of LAQGSM03 for these fission cross sections practically coincide with the ones by CEM03 above the GDR region, as the calculation of fission cross sections in CEM03 and LAQGSM03 were developed to be (see details in Reference 8), but are significantly lower than the data in the GDR region, as LAQGSM03 does not use the Kossov approximation and so should not be applied in the GDR region. Results of CEM95, CEM98, and CEM2k are also below the data in the GDR region, for the same reason.

We note that all the CEM03 and LAQGSM03 results shown in Figure 6 and in the following figures are obtained using default and fixed values of all parameters, without fitting anything. We only specify the energy of the incident photons and A and Z of the target in the inputs to CEM03 (and CEM2k+GEM2) and LAQGSM03, and then calculate. CEM95, CEM98, and CEM2k

use a parameter whose value affects drastically the calculated fission cross sections, just as in many similar statistical models: This is the ratio of the level density parameters used in the fission and evaporation channels, a_f/a_n (or, B_s , in the case of CEM98, see details in Reference 158). The fission cross sections calculated by any code employing the statistical evaporation and fission models depend so much on a_f/a_n that by fitting this ratio to available data it is possible to get a good agreement with the measured data (but not to predict unmeasured fission cross sections) with any reasonable values for the fission barriers, nuclide masses, pairing energies, and deformations, for any particular measured reaction. This is why some published papers that analyze fission cross sections or even pretend to obtain “experimental fission barriers” without addressing the question of a_f/a_n are of low significance. In our CEM95, CEM98, and CEM2k calculations, we use the default options for nuclear masses, pairing energies, and fission barriers (the “recommended” options, in the case of CEM95, where several options are available in its input; see details in Reference 27), but we still need to define (more exactly, to fit) the values of

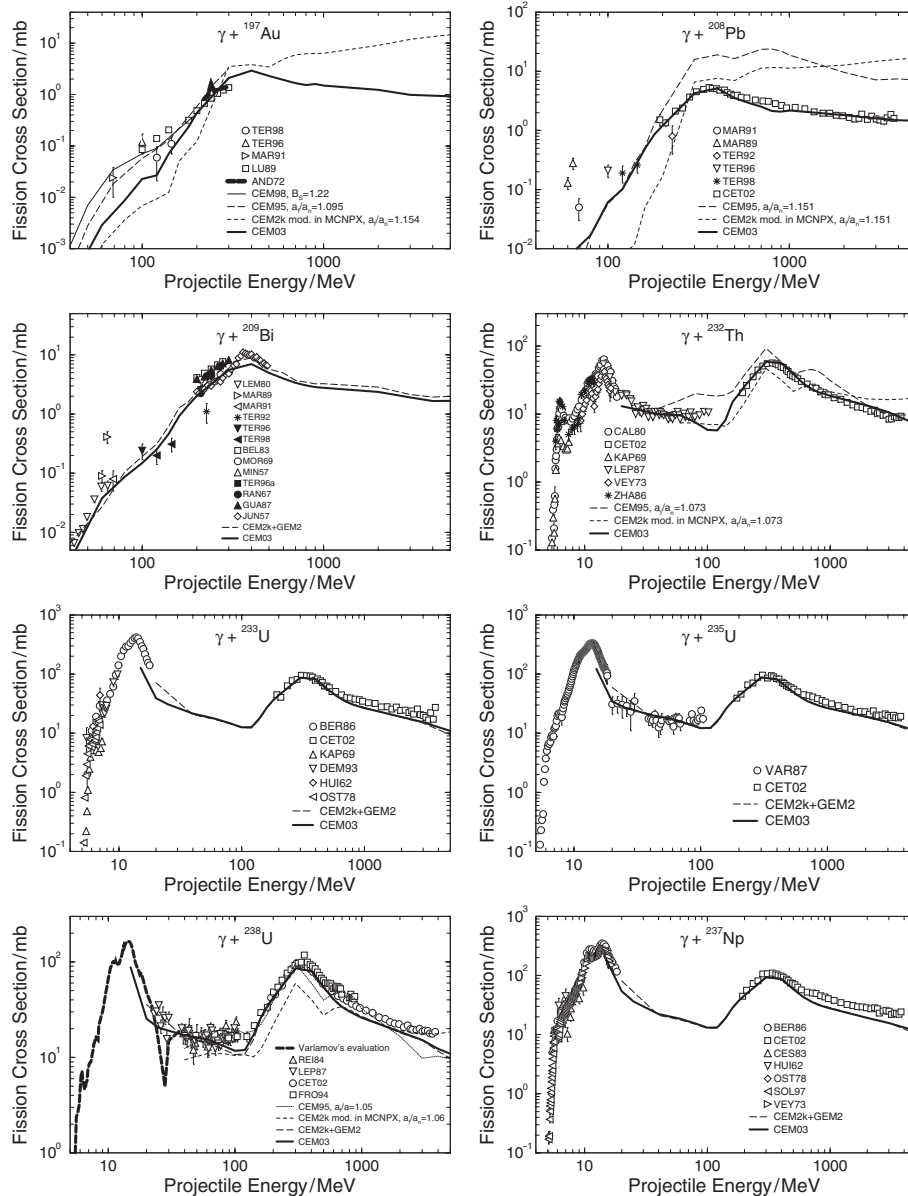


Figure 6. Comparison of the calculated photofission cross sections on ${}^{197}\text{Au}$, ${}^{208}\text{Pb}$, ${}^{209}\text{Bi}$, ${}^{232}\text{Th}$, ${}^{233}\text{U}$, ${}^{235}\text{U}$, ${}^{238}\text{U}$, and ${}^{237}\text{Np}$ with the experimental data (symbols), results by the previous versions of CEM (see details and references in the text), and the statistical evaluation by Varlamov et al. from independent measurements,¹⁵⁹ as indicated. Experimental data are from: TER98,¹⁴⁵ TER96,¹⁴⁴ MAR89,¹⁴⁶ MAR91,¹⁴⁷ LU89,¹⁶⁰ AND72,¹⁶¹ TER92,¹⁶² CET02,¹⁶³ LEM80,¹⁶⁴ BEL83,¹⁶⁵ MOR69,¹⁶⁶ MIN57,¹⁶⁷ TER96a,¹⁶⁸ RAN67,¹⁶⁹ GUA87,¹⁷⁰ JUN57,¹⁷¹ CAL80,¹⁷² KAP69,¹⁷³ LEP87,¹⁷⁴ VEY73,¹⁷⁵ ZHA86,¹⁷⁶ BER86,¹⁷⁷ DEM93,¹⁷⁸ HUI62,¹⁷⁹ OST78,¹⁸⁰ VAR87,¹⁸¹ REI84,¹⁸¹ FRO94,¹⁸² CES83,¹⁸³ OST78,¹⁸⁰ and SOL97.¹⁸⁴

a_t/a_n (or, B_s , in the case of CEM98): These values are listed on our plots in Figure 6. Naturally, CEM2k+GEM2, CEM03, and LAQGSM03 also had the problem of a_t/a_n in the beginning, but this problem was solved in Reference 8 by fitting these parameters for proton-induced measured fission cross sections for all targets for which we found data, at all incident energies, and by their extrapolation/interpolation for unmeasured targets. The fitted values are fixed and are used in all our further CEM03 and LAQGSM03 calculations without subsequent variation; this allows us not only to describe well most of the measured data but also to predict reasonably well unmeasured fission cross sections. The fitting procedure⁸ was done so that both CEM03 (and CEM2k+GEM2) and LAQGSM03 describe as well as possible all available proton-induced measured fission cross sections; this is why the fission cross sections calculated by CEM03 practically coincide with the ones obtained by LAQGSM03 and with the experimental data.

We note that both CEM03 and LAQGSM03 assume that the reactions occur generally in three stages (see e.g. Reference 185). The first stage is the IntraNuclear Cascade (INC), in which primary particles can be re-scattered and produce secondary particles several times prior to absorption by, or escape from the nucleus. When the cascade stage of a reaction is completed, both

our codes use the coalescence model described in Reference 186 to “create” high-energy d, t, ${}^3\text{He}$, and ${}^4\text{He}$ by final-state interactions among emitted cascade nucleons, already outside of the target. The emission of the cascade particles determines the particle-hole configuration, Z , A , and the excitation energy that is the starting point for the second, pre-equilibrium stage of the reaction. The subsequent relaxation of the nuclear excitation is treated in terms of the modified exciton model of pre-equilibrium decay followed by the equilibrium evaporation/fission stage of the reaction. Generally, all four components may contribute to experimentally measured particle spectra and other distributions. But if the residual nuclei after the INC have atomic numbers with $A \leq 12$, both CEM03 and LAQGSM03 use the Fermi break-up model described in Reference 10 to calculate their further disintegration instead of using the preequilibrium and evaporation models. The Fermi break-up is much faster than, and gives results very similar to, the continuation of the more detailed models to much lighter nuclei.

Figures 7 and 8 show two examples of proton spectra calculated by CEM03 and LAQGSM03 compared with the experimental data for the reactions 300 MeV $\gamma + \text{Cu}^{187}$ and 198 MeV $\gamma + \text{C}$,¹⁸⁸ respectively. Both codes describe quite well the proton spectra in the case of copper, but less well for carbon.

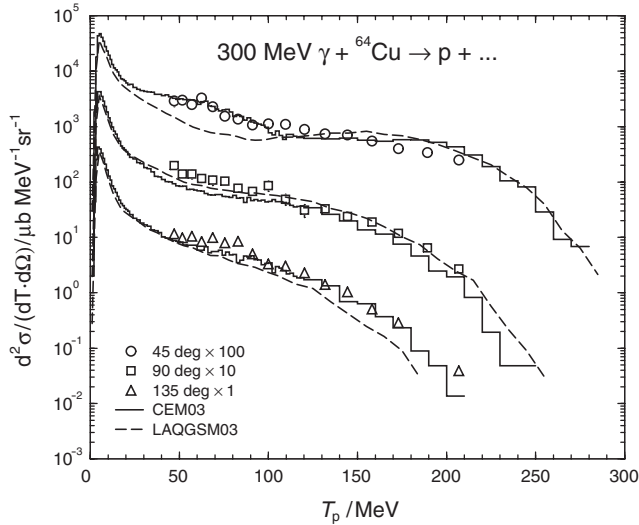


Figure 7. Proton spectra at 45°, 90°, and 135° from the reaction 300 MeV $\gamma + \text{Cu}$. Symbols are experimental data from Ref. 187, histograms and dashed lines are results of CEM03 and LAQGSM03, respectively.

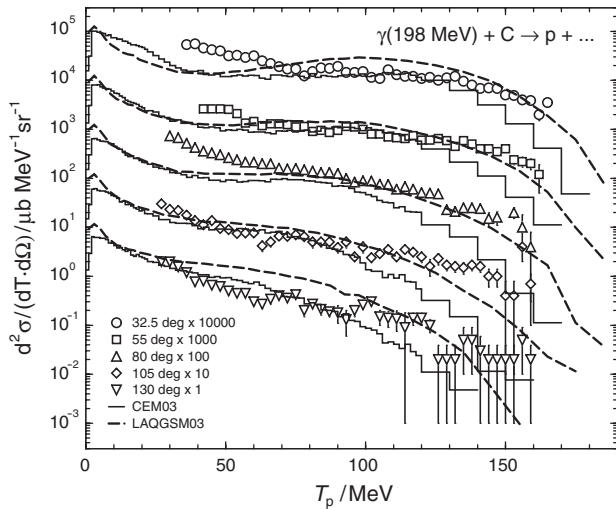


Figure 8. Proton spectra at 32.5°, 55°, 80°, 105°, and 130° from the reaction 198 MeV $\gamma + \text{C}$. Symbols are experimental data from Ref. 188, histograms and dashed lines are results from CEM03 and LAQGSM03, respectively.

Figure 9 shows examples of π^+ angular distributions from 213 MeV γ 's interacting with Pb, Sn, Ca, and C targets. One can see that the π^+ angular distributions calculated by CEM03 agree reasonably well with the experimental data¹⁸⁹ for C, Ca, and Sn targets, but underestimate by a factor of 2 to 3 the Pb data. We do not have a good understanding of this disagreement. One possible explanation of this would be if CEM03 absorbs too strongly the low-energy pions produced in γp collisions inside the target. The heavier the target the bigger would be this effect, therefore we may see it with Pb but not observe it for C, Ca, and Sn targets. There also could be problems with the experimental data for Pb. As noted in Reference 189, there is a systematic error in these data associated with the correction for the electron contamination in the yield for the forward detectors with $Z \geq 20$ targets. For instance, because of the magnitude of this background, no experimental cross sections are reported for the Pb target at 51°.¹⁸⁹

We now consider another type of photonuclear reaction, induced by bremsstrahlung photons. In contrast to reactions induced by monoenergetic photons of a given energy E , the bremsstrahlung beam is produced by monoenergetic electrons and has a spectrum of photon energies E of the form $N(E, E_0) \sim 1/E$,¹⁹⁰ from 0 to E_0 , where the end-point energy E_0 is the

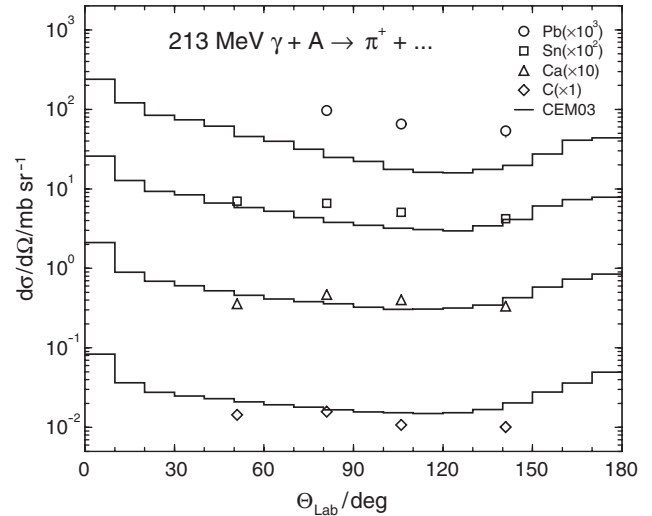


Figure 9. Energy-integrated angular distributions $d\sigma/d\Omega$ of π^+ emitted from 213 MeV γ interactions with Pb, Sn, Ca, and C. Symbols show experimental data by Fissum et al.¹⁸⁹ while histograms show CEM03 results.

maximum energy of photons produced by the given electron beam. In addition, all the experimental characteristics for reactions induced by bremsstrahlung photons are normalized per “equivalent quanta”, Q , defined as:

$$Q = \frac{1}{E_0} \int_0^{E_0} E \cdot N(E, E_0) dE \Big/ \int_0^{E_0} N(E, E_0) dE. \quad (12)$$

As discussed above, CEM03 and LAQGSM03 do not describe properly photonuclear reactions in the GDR region, we can calculate bremsstrahlung reactions with our codes while limiting ourselves to photon energies only above the GDR region.

This means that we need to simulate the energies of the bremsstrahlung photons according to their spectrum $N(E, E_0) \sim 1/E$ up to E_0 not from 0, but from a value E_{min} , above the GDR region in our calculations, and we need to use E_{min} for the lower limits of the integrals in eq 12 instead of 0 in calculating the number of equivalent quanta Q . This is easy to do in our Monte Carlo calculations. After simulation of N_{in} numbers of interactions of bremsstrahlung gammas of energy E_i with a nucleus, the number of equivalent quanta Q will be:

$$Q = \frac{1}{N_{\text{in}} E_0} \sum_i E_i = \frac{\langle E \rangle}{E_0}, \quad (13)$$

where the mean energy of the bremsstrahlung photons $\langle E \rangle$ is equal to

$$\langle E \rangle = \frac{\int_{E_{\text{min}}}^{E_0} E \cdot N(E, E_0) dE}{\int_{E_{\text{min}}}^{E_0} N(E, E_0) dE} = \frac{\sum_i E_i}{N_{\text{in}}}, \quad (14)$$

and $E_{\text{min}} \leq E_i \leq E_0$. In the present paper, we use $E_{\text{min}} = 30$ MeV for all the reactions we discuss. The total inelastic (photoabsorption) cross section σ_{in} in the case of bremsstrahlung photons is calculated as following:

$$\sigma_{\text{in}} = \frac{\int_{E_{\text{min}}}^{E_0} \sigma_{\text{in}}^{\gamma}(E) \cdot N(E, E_0) dE}{\int_{E_{\text{min}}}^{E_0} N(E, E_0) dE} = \frac{\sum_i \sigma_{\text{in}}^{\gamma}(E_i)}{N_{\text{in}}}, \quad (15)$$

where $\sigma_{\text{in}}^{\gamma}(E_i)$ is the photoabsorption cross section by a nucleus of a photon with $E_{\gamma} = E_i$, simulated in a particular Monte Carlo event i .

By using here a value of 30 MeV instead of 0 for E_{min} , we will miss the products from interaction of γ with energies

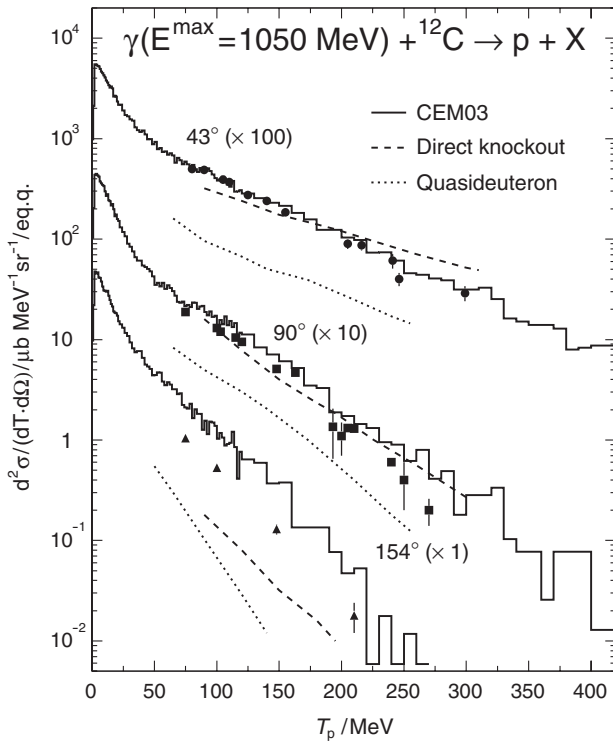


Figure 10. Comparison of measured¹⁹¹ differential cross section for proton photoproduction on carbon at 43°, 90°, and 154° by bremsstrahlung photons with $E^{\max}(=E_0) = 1.05$ GeV (symbols) with CEM03 calculations (histograms) and predictions by the direct knockout model¹⁹² (dashed lines) and a quasideuteron calculation¹⁹³ (dotted lines), respectively. The experimental data and the results by the direct knockout and quasi-deuteron models were taken from Figure 5 of Ref. 192.

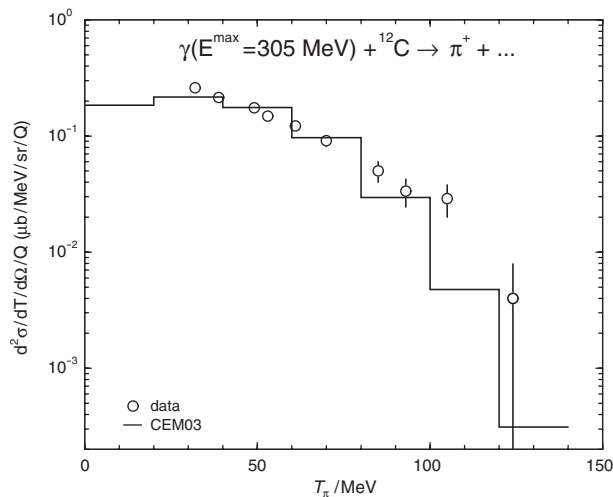


Figure 11. Comparison of measured¹⁹⁴ differential cross section for π^+ photoproduction on carbon at 90° by bremsstrahlung photons with $E^{\max}(=E_0) = 305$ MeV (circles) with CEM03 calculations (histogram).

below 30 MeV, like the cross sections for (γ, n) , $(\gamma, 2n)$, and, to a certain degree, (γ, np) in our results, but this limitation does not affect at all the description of products in the deep spallation, fission (for preactinides), and fragmentation regions, as well as the pion photoproduction and spectra of nucleons and complex particles at energies above the evaporation region.

Figures 10 and 11 present examples of proton and π^+ spectra from bremsstrahlung interaction with carbon at $E_0 = 1050$ and 305 MeV, respectively. One can see that CEM03 describes well both the measured proton and pion spectra and agrees with the data better than the direct knockout model¹⁹² and the quasi-deuteron calculations¹⁹³ do.

Since the 1980s, a large number of radiochemical measurements of bremsstrahlung-induced reactions have been performed in Japan by the group of Sakamoto (see the recent reviews^{195, 196}

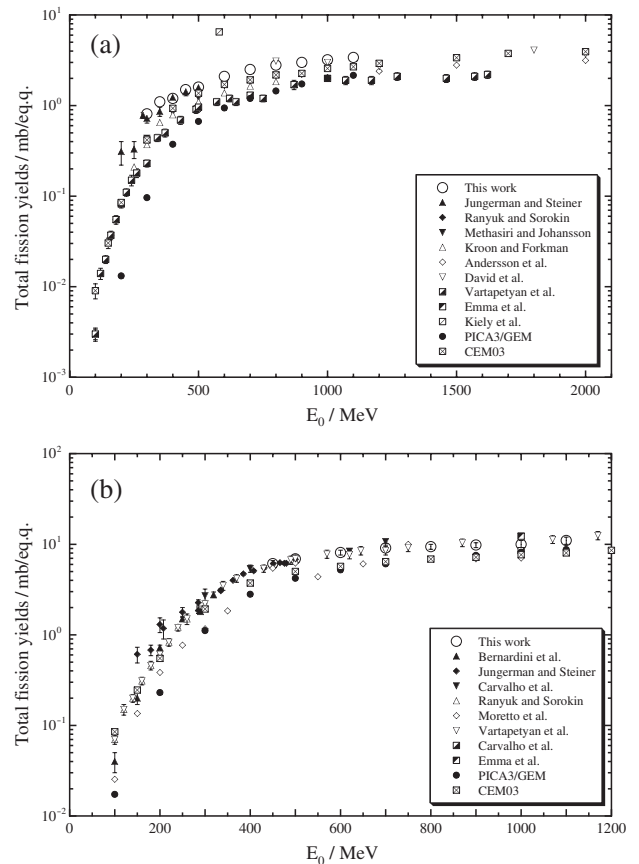


Figure 12. Bremsstrahlung-induced fission cross sections of ^{197}Au (a) and ^{209}Bi (b) as functions of the end-point energy E_0 . The experimental data for Au indicated in the insert of the figure as “This work” are from Ref. 202; other experimental data on Au are from Refs. 169, 171, and 204–209, as indicated. The data for Bi indicated as “This work” are from Ref. 203 and other data for Bi are from Refs. 166, 169, 171, 207, 208, and 210–212, as indicated. The PICA3/GEM²⁰¹ results shown with filled circles are from Ref. 203; our present CEM03 results are shown with crossed squares. We thank Haba for making this figure for us by adding our CEM03 results to Figure 19 of the review.¹⁹⁵

and references therein). Thousands of useful product cross sections were measured by this group on target nuclei from ^7Li to ^{209}Bi at bremsstrahlung end-point energies E_0 from 30 MeV to 1.2 GeV, including photopion reactions, fragmentation and fission of preactinides, deep spallation reactions, and recoil studies (mean kinetic energy and the forward/backward (F/B) ratios of products). The authors of these measurements have analyzed most of their data with the PICA code by Gabriel et al.^{197, 198} with its improved version PICA95,^{199, 200} as well as with its latest version, PICA3, merged²⁰¹ with the GEM evaporation-fission code by Furihata⁹ mentioned above, i.e. PICA3/GEM.

Recently, this group provided us with numerical values of some of their measured reactions and we have calculated them with CEM03. Figure 12 shows an example of the comparison of CEM03 results with data for bremsstrahlung-induced fission cross sections of ^{197}Au ²⁰² and ^{209}Bi ,²⁰³ compared as well with other available experimental data for Au^{169, 171, 204–209} and for Bi,^{166, 169, 171, 207, 208, 210–212} and with results by PICA3/GEM²⁰¹ from Reference 203. There is a reasonable agreement of the CEM03 results with the experimental data in the whole interval of E_0 measured, from the threshold to the highest measured energy.

Figure 13 presents the experimental data^{202, 203, 213–216} and the calculations by PICA3/GEM²⁰¹ and by CEM03 for the mass yields of products produced by bremsstrahlung reactions on ^{197}Au and ^{209}Bi at $E_0 = 1$ GeV. For convenience, all the isotopes produced in these reactions were divided into four groups, namely: 1) spallation products produced by sequential emission of several nucleons, positive pions, and complex

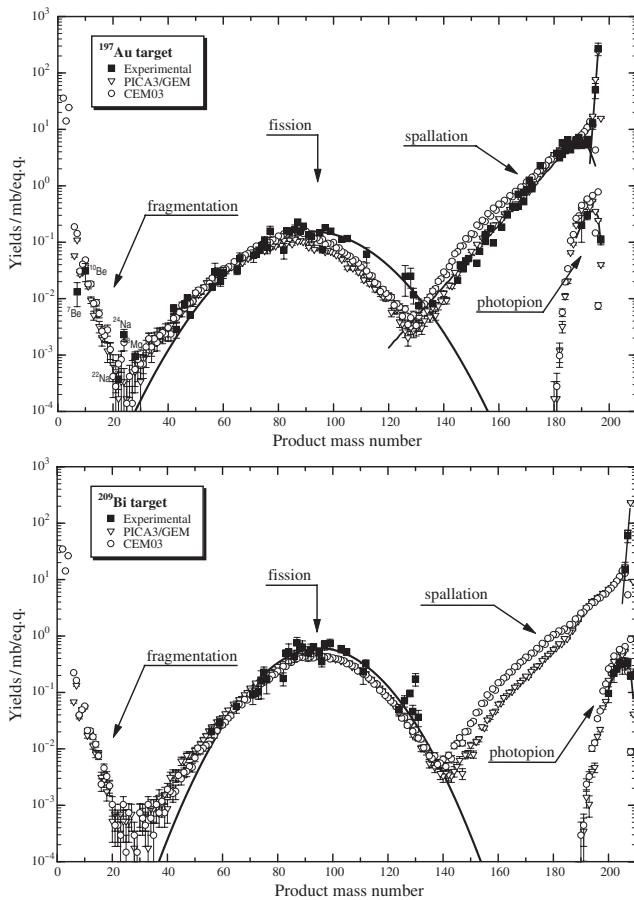


Figure 13. Comparison of CEM03 results for the mass yields of products produced by bremsstrahlung reactions on ^{197}Au and ^{209}Bi at $E_0 = 1$ GeV with the experimental data^{202, 203, 213–216} and the calculations by PICA3/GEM.²⁰¹ The experimental yields from fission of ^{197}Au and ^{209}Bi are from Ref. 213; those by spallation on ^{197}Au are from Refs. 214 and 216; those by fragmentation of ^{197}Au are from Ref. 215; the PICA3/GEM results are from several publications of Sakamoto's group and are presented in Figure 18 of the review¹⁹⁵ with the corresponding citations. The mass yields for the fission products shown by black curves represent approximations based on the experimental data obtained in Refs. 202 and 203. We thank Matsumura for making this figure for us by adding our CEM03 results to Figure 18 of the review.¹⁹⁵

particles during the INC, followed by preequilibrium and evaporation processes; 2) intermediate-mass nuclides produced via fission of excited compound nuclei; 3) light fragments emitted either via evaporation or by “fragmentation” (Fermi break-up model, in the case of our present results), and 4) “photopion” products produced in $(\gamma, \pi^- xn)$ and $(\gamma, 2\pi^- xn)$ reactions, where the charge of the products is higher than that of the initial target. One can see that CEM03 describes quite well the yields of products in all these groups and agrees with the experimental data and results by PICA3/GEM. CEM03 does not describe well the spallation products very near the target, that are produced via (γ, xn) reactions, because it does not consider photons with energies in the GDR region ($E_{\min} = 30$ MeV), as discussed above.

Some of the experimental data points in the spallation region (in the case of ^{197}Au) are overestimated by calculations up to a factor of two or three, while some of the experimental yields in the fission region are underestimated up to a factor of five or more. We do not have yet a clear understanding of this disagreement and we plan to address it in the future. Comparing our calculation results with experimental data isotope-by-isotope, as we did earlier for proton-induced reactions (see, e.g. Reference 3 and 217 and references therein), rather than the mass distributions, may help us understand better and solve this problem. We plan to perform such an analysis of isotopic yields from photonuclear reactions in the future.

Our preliminary analysis shows that CEM03 also allows us

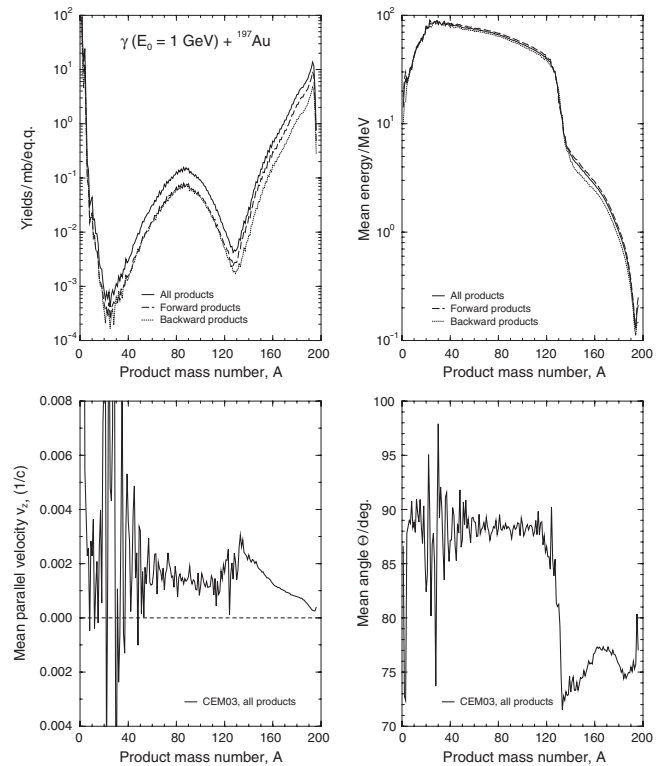


Figure 14. Results by CEM03 for 1 GeV bremsstrahlung-induced reactions on Au. Upper left plot: mass yield of all products (thick solid line), isotopes produced in the forward laboratory direction (thick long-dashed line), and backward products (thin dotted line); Upper right plot: mean laboratory kinetic energy of all products (solid line) and of only forward (long-dashed line) and backward products (dotted line); Lower left plot: mean laboratory velocity v_z of all products in the beam direction; Lower right plot: mean laboratory angle Θ of all products as a function of A . The big fluctuations in the values of v_z and Θ for masses around $A = 20$ and 130 do not provide real physical information, as they are related to the limited statistics of our Monte Carlo simulation caused by the very low yield of isotopes at the border between spallation and fission, and at that between fission and fragmentation. Our calculation provides only a few (or even one) isotopes of a given A in these mass regions, and mean values for such events do not have any significance.

to describe the recoil properties (forward and backward product yields, their F/B ratio, and mean kinetic energies) of nuclides produced in bremsstrahlung-induced reactions on medium and heavy targets at intermediate energies (see Reference 196 and reference therein). We plan to publish our analysis in a future paper. Below, we present only several predictions by CEM03 for the bremsstrahlung-induced reaction on Au at $E_0 = 1$ GeV, as we find such results informative and useful to better understand the mechanisms of nuclear reactions.

Due to the momentum transferred by the bombarding gammas to the nuclear target, one may expect that most of the spallation products would fly in the forward direction in the laboratory system. The lower-right plot in Figure 14 shows the mean laboratory angle Θ of all products as a function of A . We see that the mean angle of the spallation products is predicted by CEM03 to be between 72 and 80 degrees. (It is not equal to 0 degrees, as the probability of projectiles to have an impact parameter exactly equal to zero is equal to zero, and photons hit more often the periphery of the nucleus rather than its center.) The thick solid curve in the upper-left plot of Figure 14 shows the yield of all products as a function of A , the same results compared in Figure 13 with the experimental data and the calculations by PICA3/GEM. Besides the total yield, this plot shows also its components from nuclides produced in the forward (thick long-dashed line) and backward (thin dotted line) directions. One can see that for all the spallation isotopes, the cross sections for the forward products are about a factor of two higher than those for backward products,

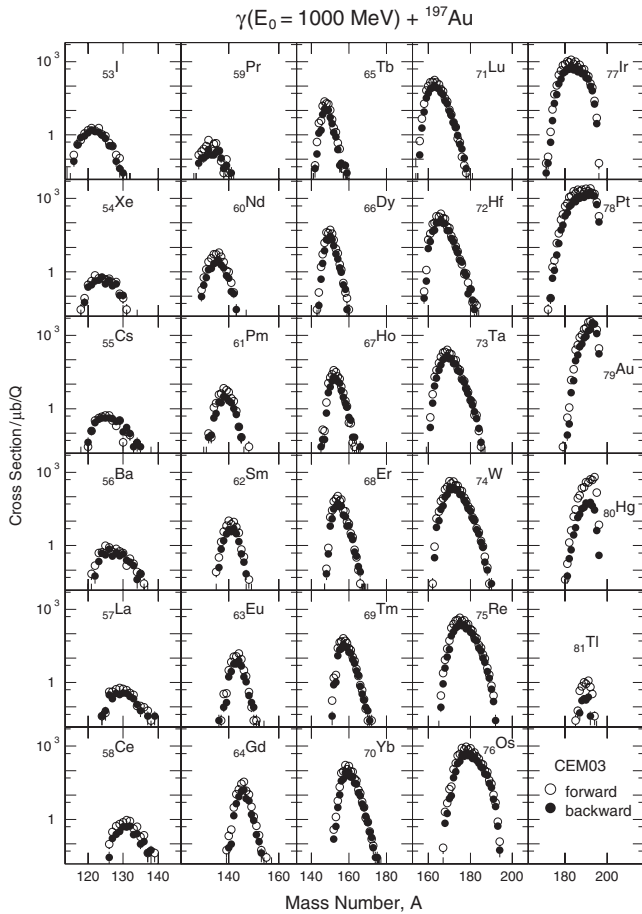


Figure 15. Predicted cross sections of the spallation products from the $E_0 = 1$ GeV bremsstrahlung photon-induced reaction on Au: Open circles show the yield of the products produced in the forward direction in the laboratory system, while the black circles show results for the backward products.

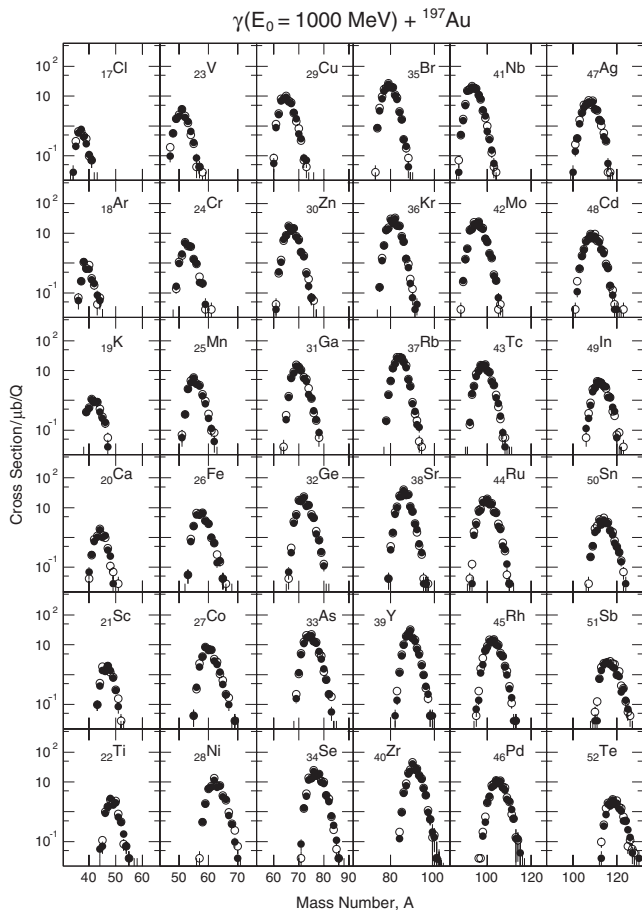


Figure 16. The same as Figure 15, but for fission and fragmentation products.

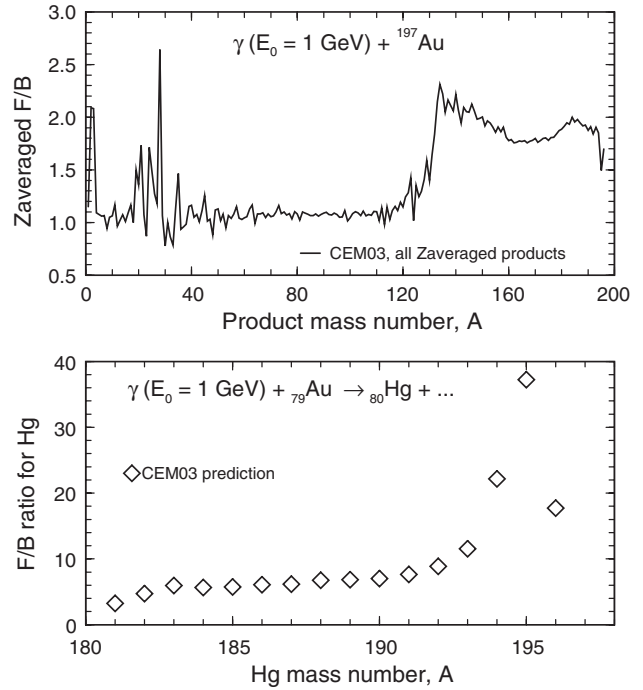


Figure 17. Upper plot: Z-averaged A-dependence of the F/B ratio of the forward product cross sections to the backward ones, as predicted by CEM03 for the reaction of $E_0 = 1$ GeV bremsstrahlung photons on Au. Lower plot: The F/B ratio of the Hg isotopes produced in the same reaction as a function of the mass number of the Hg nuclei.

in complete accordance with the available experimental data (see the review¹⁹⁶ and references therein). But the situation changes completely for fission products: The momenta of the fissioning nuclei is small, their mean kinetic energy in the laboratory system is a few MeV (see the upper-right plot in Figure 14), that is much less than the kinetic energy from several tens to about a hundred MeV that fission fragments receive due to the Coulomb repulsion of the fragments. If we neglect the effects of angular momentum, the fission fragments would be distributed isotropically in the system of the fissioning nucleus, and the small momentum of the fissioning nuclei makes this distribution almost isotropic also in the laboratory system. The upper left plot of Figure 14 shows that the predicted yields for the fission fragments in the forward and backward directions are almost the same, i.e. the F/B ratio for the fission fragments is almost equal to one, again in complete agreement with the available experimental data (see Reference 196 and references therein).

The mean kinetic energy of the forward products shown in the upper-right plot of Figure 14 is only very slightly higher than that of the backward products (the momenta of fissioning nuclei are low, as discussed above), with a little higher effect for the spallation products than for fission fragments, as is to be expected. Due to this fact and to the near isotropy of the fission fragments, some fission fragments may have their mean velocity in the direction opposite the beam, as can be seen from in the lower-left plot of this figure.

It is much more informative to study the F/B problem considering the forward and backward cross sections for every product separately, as shown in Figures 15 and 16, rather than addressing only the A-distribution of their yields. Whereas the Z-averaged A-dependence of the F/B ratio is about a factor of two for all the spallation region (see also Figure 17), the situation changes for individual isotopes. The cross sections of the forward-emitted isotopes are still about a factor of two higher than the backward cross sections for most of the spallation products, but their ratio is much higher for Hg and Tl, and depends strongly on the mass numbers of the products. Hg and Tl are “photopion” products produced via (γ, π^+xn) and $(\gamma, 2\pi^+xn)$, respectively, with emission of only a few neutrons in

addition to the pions. When the number of emitted neutrons is small, the product “remembers” the momentum transferred to the target by the projectile, and such neutron-rich products go mainly forward, with a ratio F/B up to ten or higher. On the contrary, in reactions where many neutrons are emitted approximately isotropically, the residual nucleus has lost most of its “memory” of the initial momentum. Therefore the neutron-deficient products from such reactions have a smaller F/B ratio, usually around a factor of two. The farther away from the target are the products, the smaller is this effect; for products with $Z \lesssim 70$, it practically disappears. Approaching the border around $A = 130$ of the transition between spallation and fission products, the F/B ratio decreases and for Ce, La, Ba, Cs, Xe, and I nuclei shown in the left column of Figure 15, the F/B ratio becomes almost equal to one and remains so for all the fission products shown in Figure 16.

The Z -averaged F/B ratio for all nuclides of a given A as a function of A is presented in the upper plot of Figure 17. The lower plot of this figure shows the F/B ratio for isotopes of Hg: One can see that it decreases from about thirty-seven for neutron-rich ^{195}Hg produced by the $^{197}\text{Au}(\gamma, \pi^- 2n)$ reaction to about three for neutron-deficient ^{181}Hg produced by the $^{197}\text{Au}(\gamma, \pi^- 16n)$ reaction.

We think that an analysis of such recoil characteristics is quite informative not only for photonuclear reactions, but also for proton-induced and other types of reactions. Analyses of the experimental data for such characteristics would allow us to understand better the mechanisms of nuclear reactions and may help us to distinguish the fission processes from the fragmentation (or evaporation) ones in the production of heavy fragments from reactions on medium-mass targets, like Fe (see discussion of this problem in References 1 and 2). New measurements on the recoil properties from reactions with any type of projectiles, including bremsstrahlung photons, would be very useful.

6. Conclusions

The 2003 versions of the codes CEM2k+GEM2 and LAQGSM, CEM03 and LAQGSM03, are extended to describe photonuclear reactions. Both our models consider photoproduction of at most two pions, which limits their reliable application to photon energies up to only about 1.5 GeV. The present version of our models do not consider photoabsorption in the GDR region, which defines the lower limit of the photon energy to about 30 MeV. Nevertheless, developing and incorporating of a routine based on the phenomenological systematics for the total photoabsorption cross section by Kossov into CEM03 allow us to enlarge the region of applicability of CEM03 and to get quite reasonable results for applications both in the GDR region and above 1.5 GeV.

As shown by several examples, CEM03 and LAQGSM03 allow us to describe reasonably well, and better than their precursors, many photonuclear reactions needed for applications, as well as to analyze mechanisms of photonuclear reactions for fundamental studies. But our models still have several problems. Figure 18 shows examples of such problems on proton and deuteron spectra from reactions induced by 60 MeV monoenergetic photons on Ca: One can see that both CEM03 and LAQGSM03 describe reasonably well the shape of the proton spectrum, but their absolute values differ by more than a factor of two. This is because the CEM03 results are normalized to the total photoabsorption cross section predicted

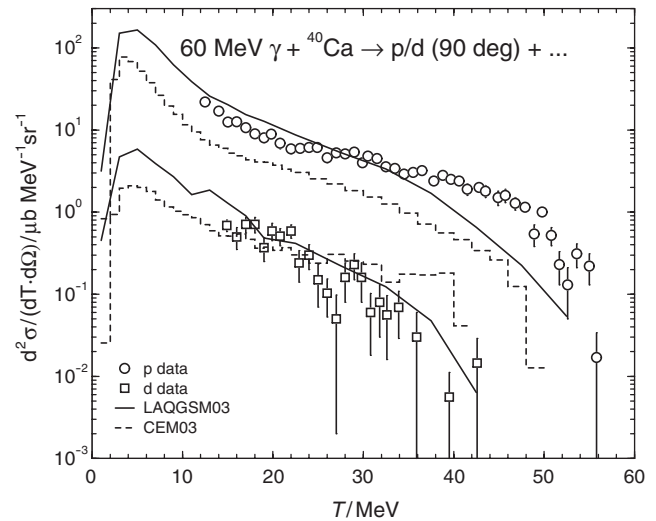


Figure 18. Examples of two problems with the current versions of our codes: proton and deuteron spectra at 90° from the reaction $60 \text{ MeV } \gamma + \text{Ca}$. Symbols are experimental data from Ref. 218, solid lines and dashed histograms are results from LAQGSM03 and CEM03, respectively. The CEM03 spectra are normalized to the total absorption cross section as predicted by Kossov’s systematics, equal to 3.49 mb for this reaction, while the LAQGSM03 spectra are normalized to the Monte-Carlo total absorption cross section calculated by that code to be equal to 8.5 mb.

by the Kossov systematics, which gives 3.49 mb for this reaction, while the LAQGSM03 results are normalized to the Monte-Carlo-calculated total photoabsorption cross section of 8.5 mb. If we refer to Figure 4, we see that the Kossov systematics for the reaction $\gamma + \text{Ca}$ predicts values that are a factor of two below the available experimental data at energies around 60 MeV. This explains the difference between the CEM03 and LAQGSM03 results shown in Figure 18, and suggest that the Kossov systematics should be further improved. Even allowing for this normalization problem, both codes appear to underestimate the cross sections for the higher-energy protons.

A further problem shown in Figure 18 is for the spectra of deuterons. The predicted spectra of deuterons differ both in their shapes and absolute values for the two codes. CEM03 and LAQGSM03 have different intranuclear-cascade models, leading after the INC stage of any reactions to different average values for A , Z , and E of the excited nuclei, as a starting point for the preequilibrium and evaporation stages of reactions, where most of the deuterons are produced. This explains the difference in the deuteron spectra predicted by the two codes and suggests that further work to improve the description of complex-particle emission is necessary.

The overestimation of the high-energy tail of the deuteron spectrum by CEM03 is partially related with an imperfect description of the preequilibrium emission of d from this reaction, due to an excessively simplified estimation of the probability of several excited nucleons (excitons) coalescing into a complex particle that can be emitted during the decay of the excited nuclei produced after the cascade.

We plan to address these problems in the future. In addition, we plan to extend our models to describe photoabsorption in the GDR region, as discussed previously, and to extend our models to describe photonuclear reactions at energies of 10 GeV or more.[†]

Our present study suggests that analysis of characteristics of

[†]Actually, after completing the manuscript of the present paper, we have extended already LAQGSM03 to describe photonuclear reactions on nuclei to higher energies, up to 10 GeV and higher. This version of LAQGSM is called LAQGSM03.01. It considers 56 different channels for elementary γp interactions and 56 channels for similar γn interactions and it is described briefly in our recent LANL paper: S. G. Mashnik, K. K. Gudima, M. I. Baznat, A. J. Sierk, R. E. Prael, and N. V. Mokhov, “CEM03.01 and LAQGSM03.01 Versions of the Improved Cascade-Exciton Model (CEM) and Los Alamos Quark-Gluon String Model (LAQGSM) Codes,” Los Alamos National Laboratory Research Note X-5-RN (U) 05-11, LANL Report LA-UR-05-2686 (2005). LAQGSM03.01 will be described in details in a separate future paper.

recoil nuclei produced by photonuclear and other types of reactions is a powerful tool to understand mechanisms of nuclear reactions. We encourage future measurements of such characteristics both for photonuclear and proton-or/and nucleus-induced reactions.

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